ADVANCED DIGITAL SIGNAL PROCESSING TECHNIQUE TO REDUCE SYSTEM COMPLEXITY USING DHT ALGORITHM

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Abstract—In this paper a new very large scale integration (VLSI) algorithm for a $2^N$-length discrete Hartley transform (DHT) that can be efficiently implemented on a highly modular and parallel VLSI architecture having a regular structure is presented. The DHT algorithm can be efficiently split on several parallel parts that can be executed concurrently. In this we present a new approach to design VLSI algorithms and VLSI architectures based on a synergistic treatment of the problems at algorithmic, architectural and implementation level. Moreover, the proposed algorithm is well suited for the sub expression sharing techniques that can be used to significantly reduce the hardware complexity of the highly parallel VLSI implementation and also it will increase the speed of the parallel multipliers. Using the advantages of the proposed algorithm and the fact that we can efficiently share the multipliers with the same constant, the number of the multipliers has been significantly reduced such that the number of multipliers is very small comparing with that of the existing algorithms. Thereby, the cost and power of the design can be reduced both in efficient implementation of transforms and reduction/removal of intermediate stages by employing different techniques. The performance overview of our proposal is that we will have efficiently replacing an faster adder and high speed multiplier in the existing algorithm of highly modular and parallel architecture, thereby resulting in significant reduction of overall power consumption, propagation delay, increases the speed and improves the overall hardware complexity of the system.

Index Terms—Discrete Hartley transform (DHT), DHT domain processing, Multiplier, fast algorithms

I. INTRODUCTION

The electronics industry has achieved a phenomenal growth over the last two decades mainly due to the rapid advances in integration technologies, large-scale systems design—in short, due to the advent of VLSI. As more and more complex functions are required in various data processing and telecommunications devices, the need to integrate these functions into a small system, package is also increasing. The level of integration as measured by the number of logic gates in a monolithic chip has been steadily rising for almost three decades, mainly due to the rapid progress in processing technology and interconnects technology.

The objective of the first design iteration is to investigate the feasibility of the selected implementation approach and estimate major system parameters, such as power consumption and chip area. Two of these functions involve discrete transforms used in many DSP applications. For example: data compression, spectrum analysis and filtering in the frequency domain. The development of VLSI technology is an important prerequisite...
for making advanced and complex digital signal processing techniques not only viable, but also economically competitive. The use of VLSI technology also contributes to increased reliability of the system. The rapid advances in the technology of VLSI with the DSP based system design and their applications are better for lower power consumption and higher efficiency and there is a growing need for designers who are current and fluent in VLSI design methodologies for DSP.

The Discrete Fourier Transform (DFT) is used in many digital signal processing applications as in signal and image compression techniques, filter banks [1], signal representation, or harmonic analysis [2]. The discrete Hartley transform (DHT) [2], [3] can be used to efficiently replace the DFT when the input sequence is real. In the literature, there are some fast algorithms for the computation of DHT [4]–[7] and some algorithms for the computation of generalized DHT [8]–[10]. There are also several split-radix algorithms for computing DHT with a low arithmetic cost. Thus, Sørensen et al. [11] and Malvar [12] proposed split-radix algorithms for DHT with a low arithmetic cost. Bi [13] proposed another split-radix algorithm where the odd-indexed transform outputs are computed using an indirect method. The classical split-radix algorithm is difficult to implement on VLSI due to its irregular computational structure and due to the fact that the butterflies significantly differ from stage to stage. Thus, it is necessary to derive new such algorithms that are suited for a parallel VLSI system.

There are also in the literature several fast algorithms that use a recursive strategy as those in [14] for discrete cosine transform (DCT) and that in [10] for generalized DHT. Since DHT is computationally intensive, it is necessary to derive dedicated hardware implementations using the VLSI technology. One category of VLSI implementations is represented by systolic arrays. There are many systolic array implementations of DHT [15]–[18]. Systolic array architectures are modular and regular, but they use particularly pipelining and not parallel processing to obtain a high-speed processing. In the literature, highly parallel solutions as those in [8] and [19] were also proposed. In [8], a highly parallel and modular solution for the implementation of type-III DHT based on a new VLSI algorithm is proposed. In [19], we have a highly parallel solution for the implementation of DHT based on a direct implementation of fast Hartley transform (FHT). It is worth to note that hardware implementations of FHT are rare.

Multipliers in a VLSI structure consume a large portion of the chip area and introduce significant delays. This is the reason why memory-based solutions to implement multipliers have been more and more used in the literature [15], [20]–[24]. To efficiently implement multipliers with lookup-table-based solutions, it is necessary that one operand to be a constant. When one of the operands is constant, it is possible to store all the partial results in a ROM, and the number of memory words is significantly reduced from 2L₂ to 2L₁.

In this brief, a new VLSI DHT algorithm that is well suited for a VLSI implementation on a highly parallel and modular architecture [27] is proposed. It can be used for designing a completely novel VLSI architecture for DHT. Moreover, using sub expression sharing technique [25] and sharing the multipliers with the same constant, the hardware complexity can be significantly reduced so the number of multipliers being very small, significantly less than that in [8]. In the proposed solution, we have used only multipliers with a constant that can be efficiently implemented in VLSI. The proposed solution is not only appealing by its high level of parallelism and by using a modular and regular structure but it can be also used to obtain a small hardware complexity by extensively sharing the common blocks. Thereby the performance comparison of multipliers for power-speed trade-off in VLSI design is explained in [28]. As the no of multipliers are reduced by sharing the same constant value, the power is reduced in the existence system design. So furthermore we want to reduce the power, improves the overall performance of the circuit design and also reducing the hardware complexity we have need to concentrate on replace the existence multipliers with a faster and an efficient low power multipliers and thereby we achieve an low power and high performance circuit design is obtained.

The rest of this brief is organized as follows. In Section II, we present a new algorithm for computing an N-point DHT. In Section III, we present an algorithm for a small-length DHT. In Section IV, we analyze the arithmetic cost, and in Section V, we present some examples of our algorithm. In Section VI, we present the new VLSI architecture with high performance multiplier. The conclusion is presented in Section VII.

II. NEW VLSI ALGORITHM FOR DHT

Let \( N \geq 4 \) be a power of two. For any real input sequence \( x(i) : i = 0, 1, \ldots, N - 1 \), the DHT\((N)\) is defined by

\[
X(k) = \text{DHT}(N) \cdot x(i) \\
= \sum x(i) \cdot \cos \left( \frac{2\pi kn}{N} \right) \quad \text{for } k = 0, 1, \ldots, N - 1
\]
Where \( \text{cas}(x) = \cos(x) + \sin(x) \). We can compute an \( N \)-length DHT using a new algorithm given by the following relations:

\[
X_N/k \{x(i)\} = X_N/2(k) \{x(2i)\} + u(0) \cdot \sin(2k\pi/N) + X_N/2(k) \{u(i)\} - u(0)/2 \cdot 2 \cdot \cos(2k\pi/N)
\]

(2)

\[
X_N(N/2 + k) \{x(i)\} = X_N/2(k) \{x(2i)\} - u(0) \cdot \sin(2k\pi/N) - X_N/2(k) \{u(i)\} - u(0)/2 \cdot 2 \cdot \cos(2k\pi/N)
\]

for \( k = 0, 1, \ldots, N/4 - 1 \)

(3)

\[
X_N(N/2 - k) \{x(i)\} = X_N/2(N/2 - k) \{x(2i)\} + u(0) \cdot \sin(2k\pi/N) - X_N/2(N/2 - k) \{u(i)\} - u(0)/2 \cdot 2 \cdot \cos(2k\pi/N)
\]

(4)

\[
X_N(N - k) \{x(i)\} = X_N/2(N/2 - k) \{x(2i)\} - u(0) \cdot \sin(2k\pi/N) + X_N/2(N/2 - k) \{u(i)\} - u(0)/2 \cdot 2 \cdot \cos(2k\pi/N)
\]

for \( k = 1, \ldots, N/4 \)

(5)

\[
N/2 - 1
\]

\[
X_N/2(k) \{x(2i)\} = \sum_{i=0}^{N/2 - 1} x(2i) \cdot \text{cas}[2ki \pi N/2]
\]

(6)

\[
N/2 - 1
\]

\[
X_N/2(k) \{u(i)\} = \sum_{i=0}^{N/2 - 1} u(i) \cdot \text{cas}[2ki \pi N/2]
\]

(7)

are DHT of length \( N/2 \), with \( \{u(i) : i = 0, 1, \ldots, N/2 - 1\} \) an auxiliary input sequence given by

\[
u(N/2 - 1) = x(N - 1)
\]

(8)

\[
u(i) = x(2i + 1) - u(i + 1) \quad \text{for } i = N/2 - 2, \ldots, 1, 0.
\]

(9)

For the computation of (2)–(5), there are necessary extra \( 7N/4 \) additions and \( N/2 \) multiplications, if we share the multipliers with the same constant. For the computation of the auxiliary input sequence using (8) and (9), there are necessary extra \( N/2 - 1 \) additions.

The obtained algorithm can be used as a VLSI algorithm where the number of multipliers can be significantly reduced by sharing the multipliers with the same constant as will be shown in Section VI. The number of multipliers can be further reduced using sub expression sharing techniques and the sharing of multipliers with the same constant, as shown in Section VI.

**TABLE I**

**COMPUTATIONAL COMPLEXITY**
III. ALGORITHM FOR A SMALL DHT

An efficient implementation of a fast DHT algorithm closely depends on an efficient algorithm for a small DHT. We present here an efficient DHT algorithm for a length $N = 8$.

\[
X(0) = [(x(0) + x(4)) + (x(2) + x(6))] + [(x(1) + x(5)) + (x(3) + x(7))]
\]
\[
X(2) = [(x(0) + x(4)) - (x(2) + x(6))] + [(x(1) + x(5)) - (x(3) + x(7))]
\]
\[
X(4) = [(x(0) + x(4)) + (x(2) + x(6))] - [(x(1) + x(5)) + (x(3) + x(7))]
\]
\[
X(6) = [(x(0) + x(4)) - (x(2) + x(6))] - [(x(1) + x(5)) - (x(3) + x(7))]
\]
\[
X(1) = [x(0) - x(4)] + [x(2) - x(6)] + c [x(1) - x(5)]
\]
\[
X(3) = [x(0) - x(4)] - [x(2) - x(6)] + c [x(3) - x(7)]
\]
\[
X(5) = [x(0) - x(4)] + [x(2) - x(6)] - c [x(1) - x(5)]
\]
\[
X(7) = [x(0) - x(4)] - [x(2) - x(6)] - c [x(3) - x(7)]
\]

with $c = \sqrt{2}$.

We have $M_{DHT(8)} = 2$ and $A_{DHT(8)} = 16$ as defined in the following. Due to the fact that we have to multiply with the same constant “$c$,” we can share the same multiplier, thus further reducing the number of multipliers.

IV. ARITHMETIC COST

Let $A_{DHT(N)}$ and $M_{DHT(N)}$ denote the number of additions and multipliers for computing DHT ($N$). We have

\[
M_{DHT(N)} = 2M_{DHT(N/2)} + (1/2)N \quad (10)
\]
\[
A_{DHT(N)} = 2A_{DHT(N/2)} + (9/4)N - 1 \quad (11)
\]

Where $MDHT(8) = 2$ and $ADHT(8) = 16$. Solving the recursions (10) and (11), we obtain

\[
M_{DHT(N)} = N(\log_2 N - 5)/2 \quad (12)
\]
\[
A_{DHT(N)} = 9/4N \log_2 N - 39/8N + 1 \quad (13)
\]

Table I lists the required number of multiplications and additions for the proposed algorithm, the Sorensen and Bi algorithm, where rotations are implemented with four multiplications and two additions (Radix-2[13]*) and with three multiplications and three additions (Radix-2 [13 **]).

The values of $M$ in the proposed algorithm are computed considering that the multipliers with the same constant are shared. The number of multipliers in Sorensen algorithm [11] is significantly greater than that in the proposed one. The number of multipliers for Bi algorithm where rotations are implemented with four multiplications and two additions is greater than the necessary number of multipliers for our algorithm and slightly smaller when the rotations are implemented with three multiplications and three additions. However, the split-radix algorithm has an irregular structure and is difficult to be implemented in hardware as opposed to our algorithm that has a regular and modular structure and can be very easily implemented in parallel as it will be shown in Section VI for a DHT of length $N = 32$. Moreover, the number of multipliers in the proposed implementation can be significantly further reduced by sharing multiplications as shown in Section IV.

V. EXAMPLE OF THE PROPOSED ALGORITHM

We shall illustrate the main features of the proposed algorithm considering a DHT of length $N = 32$. We first compute recursively the auxiliary input sequences

A. DHT of Length $N = 32$

\[
u(0)(15) = x(31) \quad (14)
\]
\[
u(0)(i) = x(2i + 1)) - u(0)(i + 1) \quad (15)
\]

for $i = 0, 1, \ldots, 14$
These equations have been obtained by a further reformulation of the equations obtained directly from (2)–(5) in such a way that we can extensively use the technique of sub expression sharing [18] and sharing the multipliers with the same constant. Thus, the number of multipliers has been significantly reduced at only 16, a significantly lower value than the theoretical value 40 from Table I that has been obtained using (2)–(5) without using the aforementioned technique. As can be seen, the proposed VLSI algorithm has a very good potential for using hardware sharing techniques, and many sub expressions have been used in common. We can thus significantly reduce the hardware complexity of the VLSI implementation. Moreover, due to the fact that the same constant is used in several multiplications, we can use the technique of sharing the multipliers with the same constant. Having only multiplications with a constant, we can efficiently implement these multipliers in VLSI.

VI. HIGHLY PARALLEL VLSI ARCHITECTURE

In order to clearly illustrate the features and advantages of the proposed algorithm, the VLSI architecture for a DHT of length \( N = 32 \) is presented in Fig. 1(a) and (b). It can be seen that the proposed architecture is highly parallel and has a modular and regular structure being formed of only a few blocks: U, MUL, ADD/SUB, XCH, and a few additional adders/subtracters. The “U” blocks implement (20), XCH blocks interchange the values and are simply implemented in hardware by appropriate wiring, and MUL blocks are used to implement the shared multipliers with a constant. This block contains four multipliers with a constant. Each multiplier is shared by four input sequences that are multiplied with the same constant in an interleaved manner using multiplexers and demultiplexers controlled by two clocks.

![Flow diagram for DHT algorithm](image)
One of the advantages of this algorithm and architecture is the fact that the multiplications with the same constant are shared in the MUL blocks. Thus, the number of multipliers is significantly less than the value 40 given in Table I which has become now only 16. The final values \( Y(k) \) of Section A and \( Y_0(k) \) of Section B are finally added to obtain the output sequence \( \hat{Y}(k) \) using an additional adder not presented in Fig. 1 for simplicity. The proposed architecture has a high throughput of 32 samples per clock and can be pipelined. It is highly parallel using a low hardware complexity structure. The multipliers with a constant in MUL blocks can be efficiently implemented in hardware using the techniques proposed in [20]–[24]. Parallel processing is one of the major ways to reduce power consumption, the high processing speed being traded off for low power using the reduction of the supply voltage value [26]. The required control structure is very simple which is another important advantage.

We define another module as

\[
U_0(k) \{xa(i)\} = Xs(k) \{xa(i)\} - xa(0)/2. \tag{20}
\]

In the proposed system it is aimed to reduce the power consumption, improve the performance of the system and also reduces the system complexity of the DSP based VLSI circuit using Discrete Hartley transform. The multipliers play a major role in arithmetic operations in digital signal processing applications. The present development in processor designs aim at low power multiplier architecture usage in their processor circuits. So, the need for low power multipliers has increased. Hence the designers concentrate more on low power efficient circuit designs. Generally the computational performance of DSP processors is affected by its multipliers performance.

Hence we can put over a solid care to overcome those drawbacks using our design. Processors efficiency is usually determined from its multiplier speed and supply voltage. Therefore the high performance multiplier is used for obtaining the low power and the basic algorithms are used to increase the speed of the parallel multipliers. Thus to speed up the processor mostly a parallel multiplier can be used comparative to serial multipliers for better performance.

By replacing shared constant multipliers with faster one's we have to predict that further reduction of power will occur. In this proposed system the same 32 point DHT architecture will be considered to prove power reduction. As the no of multipliers are reduced by sharing the same constant value, the power is reduced in the existence system. So furthermore we want to reduce the power, improves the overall performance of the circuit design and also reducing the hardware complexity we have need to concentrate on replace the existence multipliers with a faster and an efficient low power multipliers and thereby we achieve an low power and high performance circuit design is obtained.

![Fig. 2 Overall project flow diagram](image-url)
VII. CONCLUSION

In this paper a new highly parallel VLSI algorithm for the computation of a length N=2^n DHT having a modular and regular structure has been presented. Moreover, this algorithm can be implemented on a highly parallel architecture with a low hardware complexity by extensively using a sub expression sharing technique and the sharing of multipliers having the same constant and therefore the design consumes less power. The main feature of the suggested system is reduced area, power and high throughput. The DHT algorithm was developed by using Modelsim and some of the parameters of the design are viewed in the simulation process. This simulation view gives the correct logic of our DHT algorithm design and it is synthesized using Altera Quartus II tool. The synthesis result shows the total number of gates used, total power dissipation, speed and time are obtained. Compared to the best of other existing designs our proposed design is better for speed and power consumption. Thus the proposed system consists of an effective architecture with efficient and adaptive nature. Thereby, in this the no of multipliers are reduced by sharing the same constant value so the power is reduced and further one we have to achieve an more power efficient, high speed, low power dissipation and reduce the complexity of the design by replacing the shared constant multipliers with the high performance, high speed and low power multipliers.

REFERENCES


