



# Unsupervised Learning on Cosmic Ray Daily Harmonic Variations

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*Abstract: Clustering is division of data into groups of similar objects. From a machine learning perspective cluster correspond to hidden patterns. In unsupervised learning we find cluster to represent a data concept. Since scientific organizations also generate large volumes of data, the challenges are to analyze the data using the recent data mining techniques, so as to arrive at meaningful conclusions. For real life applications, we have used the hourly cosmic ray intensity data from 1965 to 2006 to first derive for each day, the amplitude and phase of the harmonics of the daily variation ( $r_1$ ,  $\phi_1$ , and  $r_2$ ,  $\phi_2$ ). We have applied the k-mean partitioning algorithm, the agglomerative hierarchical clustering algorithm BIRCH, and the density based partitioning algorithm DBSCAN on the above set of daily data containing  $r_1$ ,  $\phi_1$ , and  $r_2$ ,  $\phi_2$  for each day. Many interesting clusters have been identified. The cluster analysis indicates that a very clear-cut 10-11 year periodicity is observed in the harmonics dataset even when all the four attributes are considered together. Moreover, similar characteristics are repeated after a gap of 10-11 years and many years occurring in pairs in the two sets (out of the 4 sets, each of about 10-11 years) are the outlier years. The years 1996 and 1997 are particularly emphasized as outliers. These results are similar to that reported in literature, though by statistical methods and by considering only  $r_1$  and  $\phi_1$  and not all the four attributes taken together. As such the superiority of the mining technique is revealed in the real life situations.*

**Key Words:** Clustering, Data mining, K-mean, BIRCH, DBSCAN, Cosmic ray harmonic

## 1. Introduction

The process of grouping a set of physical or abstract object is called clustering [JMF99]. A cluster is a collection of data objects that are similar to one another within the same cluster and are dissimilar to the objects in other clusters [D93] [E93]. As a branch of statistics, cluster analysis has been studied extensively for many years. In cluster analysis main focus is on distance based cluster analysis [M96]. Many statistical analysis software packages or systems have built in feature for cluster analysis and they are being used as cluster analysis tools. These

tools are based on k-means, k-medoids, and several other methods. Some such type software packages or systems are such as S-Plus, SPSS and SAS.

In machine learning, clustering is an example of unsupervised learning [S80] [JD88]. Unlike classification, clustering and unsupervised learning do not rely on predefined classes and class-labeled examples. Due to this reason, clustering is a form of learning by observation, rather than learning by examples. A group of objects forms a class, only if it is describable by a concept [KR90] in conceptual clustering. Conceptual clustering differs from conventional clustering. Conventional clustering measures similarity based on geometric distance.

Data mining efforts have focused on finding methods for efficient and effective cluster analysis in large database. Active themes of research focus on scalability of clustering methods [G02], the effectiveness of the methods for clustering complex shapes and type of data [K01] [HKT01], high-dimensional clustering techniques, and methods for clustering mixed numerical and categorical data in large databases [F99]. A very good introduction to contemporary data mining clustering techniques can be found in the textbook [HK01].

## **2. Clustering Technique**

There are two main approaches to clustering- partitioning clustering and hierarchical clustering. The partition clustering techniques partition the database into a predefined number of clusters. This uses data partitioning algorithms, (which divide data into k subsets) such as K-Mean [H75] and K-Medoid algorithms or density based partitioning approach such as DBSCAN [EKX96], GDBSCAN [SEKX98] etc. In hierarchical clustering techniques a sequence of partitions are made in which each partition is nested into the next partition in the sequence. It creates a hierarchy of cluster from small to big or big to small. The hierarchical techniques are classified as - agglomerative and divisive clustering techniques. Agglomerative clustering techniques (such as BIRCH [ZRL96], CURE [GRS98] etc.) starts with as many clusters as there are records, with each cluster having one record. Then pair of clusters are successively merged until the number of clusters reduce to k. At each stage, the pair of clusters that are merged are the ones nearest to each other. Some of the popular hierarchical clustering algorithms are BIRCH [ZRL96], CURE [GRS98] etc. Divisive clustering techniques take the opposite approach from agglomerative techniques. Divisive clustering starts with all the records in one cluster, and then tries to split that cluster into small pieces [HK01].

### 3. Daily Variations of Cosmic Rays

Solar modulation of galactic cosmic rays is an important aspect in the studies of solar-terrestrial-relationships. While these (cosmic rays) highly energetic positively charged particles traverse the vast interplanetary medium (impinging from the outside of the heliosphere), they are continuously modulated by the solar output and its variations. As such the study of the variability of the cosmic ray particles continuously recorded by the earth based monitors, provide an easy way to understand the fast changing solar output, which modulates these galactic particles both in space and time [R72] [A83].

The spatial variations in the interplanetary space are seen by earth based monitors, in 24-hours, as daily variation (periodic in nature) of cosmic rays, superimposed on which are the aperiodic transient variations of varying magnitudes. For earth based detectors, the spatial variations are local time phenomena, whereas the transient variations are universal time phenomena which occur at the same instant of time all over the globe [L71]. As such, the variety of neutron detectors widely distributed in latitude and longitude of the earth record these transient variations almost simultaneously.

The existence of significant amplitudes of the first two harmonics of the spatial variations (i.e. the daily variations) of cosmic rays observed by neutron and meson monitors have been extensively studied for more than fifty years and their characteristics have been well reviewed in literature from time to time [PD71] [VB90] [SB06]. The pressure-corrected hourly cosmic ray intensity data from high counting rate super neutron monitors are continuously available for a number of neutron monitors since 1965, and so also for the same period, the near earth interplanetary medium parameters (in situ) such as solar wind and interplanetary magnetic field components. As such, it is instructive to study afresh the phenomena of the variability of the daily variations of cosmic rays, for the entire period from 1965 to 2006, using the amplitude and phase of the first two harmonics as a single entity, by applying the mining techniques available for the large databases.

### 4. Harmonic Variation

For obtaining the harmonics of the daily variations of cosmic rays, for each day, we have used the datasets containing hourly cosmic ray intensity from 1965 to 2006 of Kiel neutron monitor station available in the website [www.ngdc.nova.gov](http://www.ngdc.nova.gov). Before using these datasets to calculate the daily harmonic parameters  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  (where  $r_1$ ,  $\phi_1$  are the amplitude and phase of first harmonic and  $r_2$ ,  $\phi_2$  are the amplitude and phase of second harmonic), we have

performed many preprocessing steps like cleaning, transformation and integration on the selected datasets for the entire period. We have also calculated the yearly vector averages of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  from these daily harmonic variations for ‘good days’ only. For calculating the daily harmonic variations, as well as yearly vector averages, of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  we have developed a comprehensive program in Visual Basic 6.0, which also takes care to ignore a few days in each year known to be contaminated by impulsive universal time transient variations of cosmic rays, thus retaining ‘good days’ only for analysis presented here, for the entire period from 1965 to 2006.

### 5. Experimental Results

For real life application, the calculated daily harmonic variations as well as yearly vector averages of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  generated from above mentioned VB program have been used for the period of 1965 to 2006.

**Experiment 1:** We have applied the k-mean clustering algorithm to divide the daily harmonics data into k-clusters. We have chosen the different values of  $k = 4, 7, 10$  in different observations. In our observation we have selected the standardized attributes of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$ , for each day for the entire period from 1965 to 2006, to find the Euclidean distance, which is defined as

$$d(i,j) = \sqrt{(|x_{i1}-x_{j1}|^2 + |x_{i2}-x_{j2}|^2 + \dots + |x_{ip}-x_{jp}|^2)}$$

where  $x_1, x_2, \dots, x_p$  are the attributes of the objects and  $i$  and  $j$  are the objects.

In our experiments the object is represented by (Year, DayNo). Table 1 gives the summarized view of the results obtained for  $k = 7$  clusters, for the entire period of 1956 to 2006, having good days. The year wise distribution of these days, for each cluster, is plotted in fig.1, where in most cases the occurrences of the maxima and / or minima are generally separated by 10-11 years.

| ClusterID | No. of Days | Avg ( $r_1$ ) | Avg( $\phi_1$ ) | Avg( $r_2$ ) | Avg( $\phi_2$ ) | Radius of Cluster |
|-----------|-------------|---------------|-----------------|--------------|-----------------|-------------------|
| 1         | 470         | 0.9005971     | 194.7072        | 0.4939104    | 23.48623        | 3.367247          |
| 2         | 3788        | 0.308137      | 210.2084        | 0.1113115    | 87.37534        | 1.397146          |
| 3         | 1348        | 0.2094155     | 291.139         | 0.1405728    | -23.42823       | 1.756649          |
| 4         | 1519        | 0.2314179     | 82.3452         | 0.1464616    | -5.124278       | 2.005774          |
| 5         | 2171        | 0.6803712     | 209.6058        | 0.1594635    | 17.86126        | 1.737811          |
| 6         | 3408        | 0.3110979     | 197.4382        | 0.1104767    | -84.73829       | 1.422001          |
| 7         | 1832        | 0.3994687     | 204.4159        | 0.2986975    | 15.10687        | 1.860185          |

Table 1: Cluster wise averages of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  along with the radius. Here radius represents the compactness of the cluster.

**Experiment2:** Here again we have used the same dataset discussed earlier but this time we are using the standardized yearly vector averages of the  $r_1$ ,  $\phi_1$ ,  $r_2$ ,  $\phi_2$ , and applied the k-mean clustering technique ( by taking optimized  $k=7$ ). Table 2 gives the summarized view of the results obtained.

| Cluster ID | No. of Years | Years  | Avg ( $r_1$ ) | Avg ( $\phi_1$ ) | Avg ( $r_2$ ) | Avg ( $\phi_2$ ) | Radius of Cluster |
|------------|--------------|--|---------------|------------------|---------------|------------------|-------------------|
| 1          | 5            | 1965, 1976, 1977, 1986,1987  | 0.204         | 207.16           | 0.032         | 26.71            | 1.528             |
| 2          | 9            | 1966,1967, 1972, 1978, 1979, 1980, 1988, 1992, 2001                          | 0.276         | 206.70           | 0.031         | 12.64            | 1.249             |
| 3          | 3            | 1995, 1996, 1997   | 0.161         | 165.46           | 0.031         | -43.20           | 1.376             |
| 4          | 4            | 1968, 1971, 1974, 2004   | 0.312         | 212.17           | 0.045         | 27.39            | 1.046             |
| 5          | 13           | 1969, 1970, 1981, 1982, 1983, 1984, 1985, 1989, 2000, 2002, 2003, 2005, 2006 | 0.307         | 217.47           | 0.028         | 35.28            | 1.068             |
| 6          | 3            | 1968, 1973, 1975, 1985, 1993, 2004, 2005                                     | 0.294         | 198.74           | 0.016         | 33.53            | 1.594             |
| 7          | 5            | 1965, 1996, 1997, 2006   | 0.279         | 189.84           | 0.048         | -0.15            | 1.604             |

Table 2: Cluster wise averages of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$  along with the radius. Here radius represents the compactness of the cluster.

**Experiment 3:** Here again we have used the same data set as in experiment 2, and applied the agglomerative hierarchical clustering algorithm BIRCH. This technique we have used to identify the most similar as well as dissimilar years. Initially all the years are recognized as independent clusters. The years which participate in the formation of the clusters in earlier iterations will be the most similar years and the years which participate in the formation of the cluster at latter passes are recognized as the outliers. To implement this algorithm we have developed a comprehensive program in Visual Basic. The Table 3 shows the result obtained from of this algorithm.

| Iteration | ClusterID | Years            | Distance Between Clusters |
|-----------|-----------|------------------|---------------------------|
| 1         | C1        | <b>1965,1986</b> | 0.369356691837311         |
| 2         | C2        | <b>1984,1985</b> | 0.44943380355835          |
| 3         | C3        | <b>1969,2006</b> | 0.500886201858521         |
| 4         | C4        | <b>1970,2003</b> | 0.610835909843445         |
| 5         | C5        | <b>1983,1989</b> | 0.660654306411743         |
| 6         | C6        | 1966,C4          | 0.707045435905457         |
| 7         | C7        | 1980,C6          | 0.693011581897736         |
| 8         | C8        | 1981,C3          | 0.713279068470001         |
| 9         | C9        | 2000,2005        | 0.863325655460358         |
| 10        | C10       | 1982,C8          | 0.911831319332123         |
| 11        | C11       | 1987,C1          | 0.982805967330933         |
| 12        | C12       | C7, C10          | 0.984204351902008         |
| 13        | C13       | 1978,1979        | 1.02457904815674          |
| 14        | C14       | 1988,2001        | 1.03400552272797          |
| 15        | C15       | 1973,1975        | 1.07646477222443          |
| 16        | C16       | C12, C14         | 1.11020398139954          |
| 17        | C17       | 2002,C5          | 1.11371171474457          |
| 18        | C18       | 1971,1974        | 1.13175892829895          |
| 19        | C19       | 1990,C9          | 1.17439067363739          |
| 20        | C20       | 1972,1977        | 1.19488656520844          |
| 21        | C21       | C13, C16         | 1.50459170341492          |
| 22        | C22       | 2004,C18         | 1.55087602138519          |
| 23        | C23       | C17, C19         | 1.55425572395325          |
| 24        | C24       | 1992,20          | 1.58612680435181          |
| 25        | C25       | 1998,C24         | 1.62597835063934          |
| 26        | C26       | 1968,C22         | 1.76180410385132          |
| 27        | C27       | 1994,C15         | 1.78886198997498          |
| 28        | C28       | C21, C26         | 1.80191421508789          |
| 29        | C29       | C2, C23          | 1.8233550786972           |
| 30        | C30       | C28, C29         | 2.0625364780426           |
| 31        | C31       | <b>1993,C27</b>  | 2.09876656532288          |
| 32        | C32       | <b>1995,1997</b> | 2.11792087554932          |
| 33        | C33       | <b>1996,C32</b>  | 2.27046942710876          |
| 34        | C34       | <b>1967,C25</b>  | 2.46455574035645          |
| 35        | C35       | <b>1976,C31</b>  | 2.78186106681824          |
| 36        | C36       | C30, C34         | 2.8255832195282           |
| 37        | C37       | C11, C36         | 2.69106459617615          |
| 38        | C38       | <b>1999, C35</b> | 3.37300777435303          |
| 39        | C39       | C37, C38         | 3.44127893447876          |
| 40        | C40       | <b>1991, C39</b> | 4.70050859451294          |
| 41        | C41       | C33, C40         | 6.32997274398804          |

Table 3: Results obtained from agglomerative hierarchical clustering algorithm “BIRCH” when applied in the dataset of yearly vector averages of  $r_1$ ,  $\phi_1$ ,  $r_2$  and  $\phi_2$ .

**Experiment 4:** For outlier analysis, again we have taken the same dataset as in experiment 2 and 3, and applied the DBSCAN clustering technique. In this technique we have to appropriately set the parameters  $\epsilon$  for finding  $\epsilon$ -neighborhood and MinPts to see that the neighborhood is adequately dense or not. If its density does not exceed the threshold MinPts then it is marked as noise objects. Since there are only 42 objects (one for each year) so we have taken MinPts =2. We have done different observation with different  $\epsilon$  Value. The years obtained as the noise years in different observations (for different values of  $\epsilon$ ) are summarized in Table 4

| Noise years in different observations (for different values of $\epsilon$ )  |  |   |  |                        |                |
|--|--|---|--|------------------------|----------------|
| $\epsilon = 0.75$  | $\epsilon = 1$   | $\epsilon = 1.25$                                 | $\epsilon = 1.5$                         | $\epsilon = 1.75$      | $\epsilon = 2$ |
| 1968, 1971, 1972, 1973,<br>1974, 1975, 1976, 1977,<br>1978, 1990, 1991, 1992,<br>1993, 1994, 1995, 1996,<br>1997, 1998, 1999, 2004 | 1975, 1977,<br>1991, 1993,<br>1996, 1997,<br>1998, 1999,<br>2004 | 1991, 1993,<br>1996, 1997,<br>1998, 1999,<br>2004 | 1991,<br>1993,<br>1996,<br>1997,<br>1998 | 1993,<br>1996,<br>1997 | 1996,<br>1997  |

Table 4: Results obtained from DBSCAN algorithm when applied in the dataset of yearly vector averages of  $r_1, \phi_1, r_2$  and  $\phi_2$ .

**6. Results and Discussion:**

By analyzing the results presented in the above experiments from 1 to 4, many interesting patterns and periodicities have been detected. They are as follows:

- (i) A critical examination of table 1, reveals that the average values of the amplitude  $r_1$  and  $r_2$  as well as radius (radius denotes the degree of compactness of the cluster) are very high in cluster C1 in comparison to other clusters. As such, the days which belong to this cluster are the outlier days. This means that on these days of cluster C1,  $r_1, r_2, \phi_1, \phi_2$  are sparsely distributed showing un-associativeness. By observing Figure 1 (which plots the year-wise number of days distributed in different clusters), the 10-11 year periodicity have been detected in almost all the clusters, including cluster C1 which belongs to outlier days i.e. where  $r_1, \phi_1, r_2, \phi_2$  differ widely.
- (ii) By thoroughly observing column “Year” of table 2, it is apparent that most of the years of 1970’s and 1990’s are quite distributed in different clusters whereas the most of the years

of 1980's and 2000's occur together in cluster C5 and the radius of the cluster C5 is very low. It means that these years are quite similar in their characteristics. This result indicates the 10-11 year periodicity as detected in (i). Also by observing clusters C1, C6 and C7, where the radius of the clusters are relatively high, the years belonging to these clusters are either consecutive or having 10-11 year periodicity, as was seen in (i) above.

- (iii) A critical examination of the table 3, it is noticed here again that the most similar years are either consecutive or having periodicity of the order of 10-11 years. Also, most of the years of 1990's have been identified as special years (i.e. outliers).
- (iv) By observing table 4, for  $\epsilon = 0.75$ , it is seen that the most of the years of 1970's and 1990's are identified as noise years or outliers. Here again we observed the 10-11 year periodicity as detected in (i), (ii) and (iii). Also for  $\epsilon = 2.0$  the years 1996, 1997 are detected as noise years or outliers i.e. these years are significantly different than all other years when all the 4 components  $r_1, \phi_1, r_2, \phi_2$  are considered together as one entity for each year, in the entire period of study 1965-2006.

Since these results are obtained just by applying the mining methodology, it would be instructive to compare the findings with those obtained by simple statistical techniques and reported in literature [SB06], considering the four attributes  $r_1, \phi_1, r_2$  and  $\phi_2$ , one-by-one separately. It is important to underline that it is only the mining techniques, which considers all the four attributes together as one entity for each year. The results of 10-11 year periodicity, and a gap of 10-11 years in the similarity characteristics and the outliers (particularly the years 1996 and 1997), have been identified earlier by doing statistical analysis and by using only  $r_1, \phi_1$  values but not in combination with  $r_2, \phi_2$ , which comes out here only by the mining techniques so easily. As such, the experimental results 1 to 4 have proved beyond doubt the significance of the mining technique in the real life situation also.

## 7. Conclusion

Since clustering is an unsupervised learning technique, so the results obtained from (i) to (iv) must be further explored and analyzed by some of the more directed data mining techniques for better understanding of the behavior of the daily harmonic variation parameters  $r_1, \phi_1, r_2$  and  $\phi_2$ , both on a day-to-day as well as on annual average basis. In future, interplanetary medium parameters can also be clubbed for better understanding of the link between them and cosmic ray variations by using clustering techniques.

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